## SUPPLEMENTARY DATA

# Top-Down Crawl: A method for the ultra-rapid and motif-free alignment of sequences with associated binding metrics 

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Supplementary Table S1: Pseudocode of entire alignment process performed by Top-Down Crawl (TDC).

```
TDC Algorithm
    Input: Table containing standard DNA sequences (A,C,G,T) of equal length in column 1 and binding metrics
    in column 2
        df}\leftarrow\mathrm{ dataframe containing binding metrics indexed by sequence
    // Average reverse complements or copy value from partner if absent from input
    dfrcc\leftarrow Copy df and reverse complement all sequences
    df\leftarrow Append df_rc to df, group by index, and save mean for each index
    // Initialization
    df\leftarrow Insert boolean column, isAligned, filled with False, to keep track of sequences which have already
    been added to the alignment
    df\leftarrow Insert boolean column, wasRef, filled with False, to keep track of sequences which have already
    been used as a reference for adding other sequences to the alignment
    df\leftarrow Insert integer column, shift, filled with N/A, to keep track of the shift assigned to each sequence
    top}\leftarrow\mathrm{ Index of seqeunce with largest binding metric from df
    k\leftarrowlength(top)
    df[top][shift]}\leftarrow
    df[top][isAligned] \leftarrow True
    Delete reverseComplement(top) from df
    // Continue iterating until all aligned sequences have been used as a reference or until all seqeunces are
    aligned
    while (isAligned == True and wasRef == False for any row in df) and (isAligned == False for any row in
    df)
        unchecked }\leftarrow\mathrm{ Subset of df including rows where isAligned }==\mathrm{ True and wasRef == False
        ref}\leftarrow\mathrm{ Index with largest binding metric from unchecked
        refshift \leftarrowdf[ref][shift]
        SNPs}\leftarrow\mathrm{ Indices within df that are 1 mismatch away from ref and where isAligned == False
        df[SNPs][shift] \leftarrowrefshift
        df[SNPs][isAligned] }\leftarrow Tru
        Delete reverseComplement(SNPs) from df
```

```
28:
31: Delete reverseComplement(olap-I) from \(d f\)
32:
33:
34:
5: df[olap-2][isAligned] \(\leftarrow\) True
        olap \(+2 \leftarrow\) Indices within \(d f\) that
df[olap +2\(][\) shift \(] \leftarrow\) refshift +2
        df[olap +2 ][isAligned] \(\leftarrow\) True
        Delete reverseComplement(olap +2 ) from \(d f\)
        \(\mathrm{d} f[r e f][\) wasRef] \(\leftarrow\) True
    \(d f \leftarrow\) Subset of df where isAligned \(==\) True
    \(d f \leftarrow\) Pad indices of \(d f\) with "-" based on shift
    Output Save \(d f\) as a table including the padded sequence, averaged binding metric, and shift
```

Supplementary Table S2: Peak memory usage for calculation of enrichment (Riley et al., 2014; Slattery et al., 2011) and TDC, BEESEM (Ruan et al., 2017), SelexGLM (Zhang et al., 2018), or MEME (Bailey \& Elkan, 1994) based alignments, evaluated for 12 SELEX-seq datasets (Abe et al., 2015; Dantas Machado et al., 2020; Zhang et al., 2018). We also report the memory requirements for $k$-mer level enrichment calculation, since this a necessary step preceding TDC or MEME based alignment as described in the text. Data is plotted in Supplementary Figure S1.

|  | Enrichment | TDC + <br> Enrichment | BEESEM | SelexGLM | MEME + <br> Enrichment |
| :---: | :---: | :---: | :---: | :---: | :---: |
| AR | 19 GB | 20 GB | 63 GB | 116 GB | 20 GB |
| GR | 19 GB | 19 GB | 55 GB | 81 GB | 19 GB |
| MEF2B | 23 GB | 23 GB | 31 GB | 228 GB | 23 GB |
| Exd-AbdA | 18 GB | 18 GB | 15 GB | 42 GB | 18 GB |
| Exd-AbdB | 18 GB | 18 GB | 20 GB | 58 GB | 18 GB |
| Exd-Antp | 18 GB | 18 GB | 17 GB | 46 GB | 18 GB |
| Exd-Dfd | 18 GB | 18 GB | 14 GB | 35 GB | 18 GB |
| Exd-Lab | 18 GB | 18 GB | 16 GB | 47 GB | 18 GB |
| Exd-PbFI | 12 GB | 12 GB | 28 GB | 110 GB | 12 GB |
| Exd-Scr | 16 GB | 16 GB | 15 GB | 52 GB | 16 GB |
| Exd-Ubxla | 17 GB | 17 GB | 18 GB | 68 GB | 17 GB |
| Exd-UbxIVa | 18 GB | 18 GB | 16 GB | 47 GB | 18 GB |

Supplementary Table S3: Table of alignment agreements, indicating what fraction of sequences were assigned to the same shift according to TDC and a given method. Data is plotted in Supplementary Figure S1.

|  | BEESEM | SelexGLM | MEME |
| :---: | :---: | :---: | :---: |
| AR | $63 \%$ | $44 \%$ | $43 \%$ |
| GR | $68 \%$ | $74 \%$ | $56 \%$ |
| MEF2B | $86 \%$ | $85 \%$ | $57 \%$ |
| Exd-AbdA | $98 \%$ | $97 \%$ | $95 \%$ |
| Exd-AbdB | $71 \%$ | $69 \%$ | $27 \%$ |
| Exd-Antp | $73 \%$ | $67 \%$ | $34 \%$ |
| Exd-Dfd | $97 \%$ | $89 \%$ | $65 \%$ |
| Exd-Lab | $96 \%$ | $90 \%$ | $51 \%$ |
| Exd-PbFI | $85 \%$ | $83 \%$ | $72 \%$ |
| Exd-Scr | $96 \%$ | $92 \%$ | $87 \%$ |
| Exd-Ubxla | $99 \%$ | $97 \%$ | $93 \%$ |
| Exd-UbxIVa | $100 \%$ | $98 \%$ | $99 \%$ |

Supplementary Table S4: Multiple linear regression (MLR) models were trained using base sequence, minor groove width, and electro-static potential information along aligned 10 -mers to predict the log enrichment of 10-mers with a Z-score larger than 2. Models were trained using 5 -fold cross validation with elastic net regularization and the median performance across the tests is reported. Data is plotted in Figure 1.

|  | TDC | BEESEM | SelexGLM | MEME |
| :---: | :---: | :---: | :---: | :---: |
| AR | 0.84 | 0.80 | 0.83 | 0.83 |
| GR | 0.76 | 0.75 | 0.74 | 0.78 |
| MEF2B | 0.56 | 0.60 | 0.63 | 0.40 |
| Exd-AbdA | 0.67 | 0.69 | 0.70 | 0.66 |
| Exd-AbdB | 0.37 | 0.33 | 0.33 | 0.22 |
| Exd-Antp | 0.42 | 0.36 | 0.34 | 0.20 |
| Exd-Dfd | 0.65 | 0.64 | 0.59 | 0.64 |
| Exd-Lab | 0.69 | 0.66 | 0.59 | 0.40 |
| Exd-PbFI | 0.75 | 0.76 | 0.75 | 0.73 |
| Exd-Scr | 0.82 | 0.76 | 0.78 | 0.65 |
| Exd-Ubxla | 0.81 | 0.77 | 0.73 | 0.59 |
| Exd-UbxIVa | 0.85 | 0.85 | 0.84 | 0.85 |

Supplementary Table S5: Wall-clock time required for each of the methods evaluated. We also report the time requirements for $k$-mer level enrichment calculation, since this a necessary step preceding TDC or MEME based alignment as described in the text. Data is plotted in Supplementary Figure S1.

|  | Enrichment | TDC + Enrichment | BEESEM | SelexGLM | MEME + Enrichment |
| :---: | :---: | :---: | :---: | :---: | :---: |
| AR | Oh 3m 9s | Oh 3m 41s | 21h 17m 59s | 1h 26 m 0 s | Oh 11m 32s |
| GR | Oh 3m 5s | Oh 3m 40s | 19h 6m 31s | Oh 41m 6s | Oh 18m 55s |
| MEF2B | Oh 4m 1s | Oh 4m 28s | 10h 6m 30s | 4h 46m 34s | Oh 11 m 56 s |
| Exd-AbdA | Oh 1m 47s | Oh 1m 57s | 4h 24m 37s | Oh 27 m 10s | Oh 1m 53s |
| Exd-AbdB | Oh 2 m 8 s | Oh 2 m 38 s | 5h 53m 40s | Oh 35 m 27 s | Oh 3m 31s |
| Exd-Antp | Oh 2 m 2 s | Oh 2 m 22 s | 4h 59m 24s | Oh 34 m 47 s | Oh 2 m 23 s |
| Exd-Dfd | Oh 2 m 2 s | Oh 2 m 9 s | 3h 58m 42s | Oh 21 m 53 s | Oh 2 m 7 s |
| Exd-Lab | Oh 2m 23s | Oh 2m 37s | 4h 28m 12s | Oh 26 m 6 s | Oh 2 m 33 s |
| Exd-PbFI | Oh 1m 30s | Oh 2m 17s | 9 h 8 m 54 s | 1h 34 m 51 s | Oh 19m 35s |
| Exd-Scr | Oh 1m 46s | Oh 2m 1s | 4h 14m 29s | Oh 36 m 9 s | Oh 2 m 0 s |
| Exd-Ubxla | Oh 2 m 9 s | Oh 2 m 27 s | 5 h 18 m 2 s | Oh 53 m 4 s | Oh 3m 18s |
| Exd-UbxIVa | Oh 1m 51s | 0h 2 m 4 s | 4h 31m 49s | Oh 27m 14s | Oh 2 m 2 s |

Supplementary Figure S1: Violin plots of data given in Supplementary Tables S2, S3, and S5. (Violin plots of data given in Supplementary Table S4 are shown in Figure 1.)


Supplementary Figure S2: Comparison of PWMs generated from each method. The TDC PWM is generated using all 10 -mers aligned with a shift of $\pm 5$, weighting each sequence by its relative enrichment. The units of the SelexGLM method are provided in terms of $-\Delta \Delta G / R T$ as described in the original method. All others are shown in terms of bits.



|  | Exd-AbdB | Exd-Antp |
| :---: | :---: | :---: |
| TDC <br> BEESEM <br> SelexGLM <br> MEME |   |   |





Supplementary Figure S3: Violin plots showing model performance across 12 SELEX-seq datasets, using various length $k$-mers as input to TDC. MLR models were trained using base sequence, minor groove width, and electrostatic potential information along aligned $k$-mers to predict the log enrichment of $k$-mers with a Z-score larger than 2. Models were trained using 5 -fold cross validation with elastic net regularization and the median performance across the tests is reported.


## Supplementary References

Abe, N., Dror, I., Yang, L., Slattery, M., Zhou, T., Bussemaker, H. J., Rohs, R., \& Mann, R. S. (2015). Deconvolving the recognition of DNA shape from sequence. Cell, 161(2), 307-318.
Bailey, T. L., \& Elkan, C. (1994). Fitting a mixture model by expectation maximization to discover motifs in biopolymers. Proc. Int. Conf. Intell. Syst. Mol. Biol., 2, 28-36.
Dantas Machado, A. C., Cooper, B. H., Lei, X., Di Felice, R., Chen, L., \& Rohs, R. (2020). Landscape of DNA binding signatures of myocyte enhancer factor-2B reveals a unique interplay of base and shape readout. Nucleic Acids Res., 48(15), 8529-8544.
Riley, T. R., Slattery, M., Abe, N., Rastogi, C., Liu, D., Mann, R. S., \& Bussemaker, H. J. (2014). SELEX-seq: a method for characterizing the complete repertoire of binding site preferences for transcription factor complexes. In Hox Genes (pp. 255-278). Springer.
Ruan, S., Swamidass, S. J., \& Stormo, G. D. (2017). BEESEM: estimation of binding energy models using HTSELEX data. Bioinformatics, 33(15), 2288-2295.
Slattery, M., Riley, T., Liu, P., Abe, N., Gomez-Alcala, P., Dror, I., Zhou, T., Rohs, R., Honig, B., \& Bussemaker, H. J. (2011). Cofactor binding evokes latent differences in DNA binding specificity between Hox proteins. Cell, 147(6), 1270-1282.
Zhang, L., Martini, G. D., Rube, H. T., Kribelbauer, J. F., Rastogi, C., FitzPatrick, V. D., Houtman, J. C., Bussemaker, H. J., \& Pufall, M. A. (2018). SelexGLM differentiates androgen and glucocorticoid receptor DNA-binding preference over an extended binding site. Genome Res., 28(1), 111-121.

## Author Contributions

B.H.C. conceived the TDC method, independently executed the project, and wrote the manuscript. T.P.C. tested the method and provided advice on implementation. R.R. supervised the project. The authors thank Luigi Manna for help with server setup.

